

# Mechanism of superconductivity in $K_3C_{60}$

(alkali/Buckminsterfullerene/electron–phonon coupling)

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**ABSTRACT** Using electronic states and phonon states from the first-principles calculations and including both conventional electron–phonon charge coupling and Jahn–Teller coupling, we predict  $T_c$  and other superconducting properties. The only adjustable parameter in the theory is the screening length,  $R_{sc}$ . Using  $R_{sc} = 0.8$ – $1.0$  Å, we find excellent agreement with experiment for  $T_c$  (16–18 K), pressure dependence of  $T_c$  ( $\Delta T_c = -6$  to  $-10$  K for 1 GPa), and  $^{12}C$  to  $^{13}C$  isotope shift ( $\alpha_C = 0.2$ ); experimental values: 19 K,  $-7$  K, and 0.3, respectively.

A number of superconducting alkali compounds of  $C_{60}$  ( $M_3C_{60}$ ) have been synthesized (1–5), leading to transition temperatures  $T_c$  from 2.5 K to 33 K. Several quite different mechanisms (6–12) have been proposed to explain the superconductivity in these materials.

A suggestion by Lannoo *et al.* (6, 7), Johnson *et al.* (8) and Varma *et al.* (9) is that dynamic Jahn–Teller (JT) coupling involving high-frequency intramolecular vibrations strongly scatter electrons near the Fermi surface, leading to superconductivity. On the other hand, Zhang *et al.* (10) estimated various contributions to the electron–electron interaction in  $K_3C_{60}$  and argued that the  $K^+$  optical–phonon modes induce a strong attraction that is the main source of superconductivity. In addition to phonon-mediated electron–pairing mechanisms, Chakravarty *et al.* (11) and Baskaran and Tosatti (12) argue that two electrons may pair by electron–electron exchange and correlation on a single  $C_{60}$  molecule.

## Hamiltonian and Electron–Phonon Couplings

We present here a first-principles, quantitative study of the superconductivity  $K_3C_{60}$ , using the Hamiltonian equation

$$H = H_{ph} + H_e + H_{ee} + H_{eph}^Q + H_{eph}^{JT}, \quad [1]$$

where each term is defined below.

**Phonon States ( $H_{ph}$ ).** We started with the graphite force field (GraFF) developed by Guo *et al.* (13) for describing the structure, elastic constants, and phonons of graphite and intercalated graphite. Without adjustments, the GraFF leads to an excellent description of the vibrational levels of  $C_{60}$  (4% average absolute error for  $A_g$  and  $H_g$ ). The lattice constants of  $K_3C_{60}$  are within 0.1 Å of experiment (14, 15), and the predicted linear compressibilities (13) of  $K_3C_{60}$ ,  $\beta = 1.13 \times 10^{-3}$  kbar $^{-1}$ , is close to experiment (15),  $1.20(9) \times 10^{-3}$  kbar $^{-1}$ .

Using the predicted structure of fcc  $K_3C_{60}$  [ $a = 14.18$  Å, experimental (14, 15)  $a = 14.24$  Å], we calculated the 189 phonon modes (eigenvectors and frequencies) for each point of a  $6 \times 6 \times 6$  grid in the Brillouin zone. These modes partition into 174 high-frequency intramolecular bands (260–1520  $cm^{-1}$ ) plus six lattice modes (130–140  $cm^{-1}$ ) involving

tetrahedral K, three lattice modes (20–50  $cm^{-1}$ ) involving octahedral K, three  $C_{60}$  librational modes (30–40  $cm^{-1}$ ), and three acoustic phonon modes. We write  $H_{ph}$  as

$$H_{ph} = \sum_{k,j} \Omega_{kj} a_{kj}^+ a_{kj}, \quad [2]$$

where  $\Omega_{kj}$  is the frequency of mode  $j$  ( $j = 1189$ ) with momentum  $k$ .

**Electronic States ( $H_e$ ).** For  $H_e$  we fitted the local density approximation (LDA) description of the conduction band by Erwin and Pickett (16) to a tight-binding Hamiltonian

$$H_e = \sum_{i,j}^{nn} t_{ij}^{(1)} c_{mi}^+ c_{nj} + \sum_k^{nnn} t_k^{(2)} c_{mk}^+ c_{lk}, \quad [3]$$

with the nearest ( $nn$ ) and the next-nearest neighbor ( $nnn$ ) hopping matrix elements. This leads to a density of states of  $N(0) = 11.5$  [the units of  $N(0)$  are states per eV per  $C_{60}$ ] and a Fermi energy of  $E_f = 0.23$  eV. These compare well with the LDA results (16) of  $N(0) = 13.2$  and  $E_f = 0.26$  eV.

We determined the Fermi surface by calculating the states from  $H_e$  at 1,000,000 points in the Brillouin zone, evaluating the Fermi energy, and selecting 330 points within 0.001 eV of the Fermi energy.

**Dynamic Charge Coupling ( $H_{eph}^Q$ ).** Dynamic charge coupling describes the changes in the electron–ion coulomb interactions, due to vibrations (for fixed electronic orbitals). We calculated the electron–phonon coupling matrix  $M_{\mathbf{k}'\mathbf{k}j}$ , using the exact phonon eigenvectors and eigenenergies with a local Wannier orbital representation for the conduction electrons.

The charge-coupling Hamiltonian is written as

$$H_{eph}^Q = \sum_l \sum_{n\alpha} \Delta \mathbf{R}_{n\alpha} \cdot \nabla_{n\alpha} V_{ei}(\mathbf{r}_l - \mathbf{R}_{n\alpha}^{(0)}), \quad [4]$$

where  $V_{ei}(r) = \exp(-r/R_{sc})/r$  is the screened electron–ion coulomb interaction with screening length  $R_{sc}$ ,  $\mathbf{R}_{n\alpha}^{(0)}$  is the equilibrium position of the  $\alpha$ th ion in the  $n$ th unit cell, and  $\Delta \mathbf{R}_{n\alpha}$  is its displacement,

$$\Delta \mathbf{R}_{n\alpha} = \sum_{\mathbf{k}j} \sqrt{1/NM_\alpha} Q(\mathbf{k}j) \xi(\alpha|\mathbf{k}j) \exp(i\mathbf{k} \cdot \mathbf{R}_{n\alpha}^{(0)}), \quad [5]$$

where  $\xi(\alpha|\mathbf{k}j)$  is the phonon eigenvector of momentum  $\mathbf{k}$  and mode  $j$  and  $Q(\mathbf{k}j)$  is its amplitude.

Using the tight-binding picture,  $H_{eph}^Q$  simplifies to

$$H_{eph}^Q = \frac{1}{V^{1/2}} \sum_{\mathbf{k}'\mathbf{k}j} M_{\mathbf{k}'\mathbf{k}j} c_{\mathbf{k}'}^+ c_{\mathbf{k}} (a_{-\mathbf{q}j}^+ + a_{\mathbf{q}j}) \quad [6]$$

$$M_{\mathbf{k}'\mathbf{k}j} = -i \sum_{\mathbf{G},\alpha} \left( \frac{\hbar}{2\rho_\alpha \Omega_{\mathbf{q}j}} \right)^{1/2} e^{-i\mathbf{G} \cdot \mathbf{R}_\alpha} \hat{V}_{ei}(\mathbf{q} + \mathbf{G}) \xi(\alpha|\mathbf{q}j) \cdot (\mathbf{q} + \mathbf{G}) W(\mathbf{q} + \mathbf{G}; \mathbf{k}', \mathbf{k}), \quad [7]$$

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Abbreviations: LDA, local density approximation; JT, Jahn–Teller.

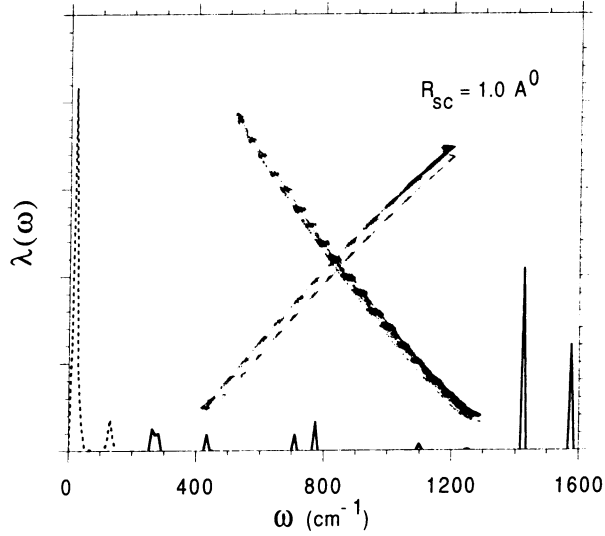


FIG. 1. Calculated values of  $\lambda(\omega) = 2\alpha^2(\omega)F(\omega)/\omega$  using both Q and JT coupling; the dashed line is for  $\lambda_Q(\omega)$ , and the solid line is for  $\lambda_{JT}(\omega)$ . For  $\omega < 200 \text{ cm}^{-1}$  all contributions are from Q, whereas for  $\omega > 200 \text{ cm}^{-1}$  essentially all contributions are from JT. The maximum value of  $\lambda(\omega)$  is 0.0669 cm.

where  $W(\mathbf{q} + \mathbf{G}; \mathbf{k}', \mathbf{k}) = \sum_{m,n=1}^3 A_m^*(\mathbf{k}') A_n(\mathbf{k}) U_{mn}$  and  $U_{mn} = \sum_i e^{-i\mathbf{k}' \cdot \mathbf{R}_i} \langle \psi_m(\mathbf{R}_i) | e^{i(\mathbf{q} + \mathbf{G}) \cdot \mathbf{r}_i} | \psi_n(0) \rangle$ . Here  $\mathbf{q} = \mathbf{k}' - \mathbf{k} + \mathbf{G}$  is in the first Brillouin zone,  $\mathbf{G}$  is a reciprocal lattice vector,  $\mathbf{A}(\mathbf{k})$  is the electronic eigenvector of momentum  $\mathbf{k}$ ,  $\mathbf{R}_\alpha$  is the equilibrium position of the  $\alpha$ th atom in the unit cell,  $\psi_m$  is a local Wannier wave function, and  $\hat{V}_{ei}(\mathbf{q}) = 1/V_0 V_{ei}(\mathbf{q})$  ( $V_0$  is the volume of a unit cell).

All quantities in Eqs. 4–7 were obtained directly from first-principles calculations except the screening length,  $R_{sc}$ . From Thomas–Fermi theory (17–19) an estimate is  $R_{sc}^{TF} = \sqrt{E_f/6\pi e^2 n_e} = 0.63 \text{ \AA}$ , where  $n_e$  is the conduction electron density and  $E_f$  is the Fermi energy for free electron gas. The proper value of  $R_{sc}$  for  $K_3C_{60}$  should be somewhat larger, perhaps 0.7–1.2  $\text{\AA}$ .

To calculate  $\lambda_Q$ , we used three  $p$ -like Gaussian functions on each  $C_{60}$  to describe approximate Wannier  $t_{1u}$  orbitals from the three electronic bands. A typical function is  $\psi_x \propto x e^{-\alpha x^2 - \beta(y^2 + z^2)}$ , with  $\alpha = 0.0397 \text{ \AA}^{-2}$  and  $\beta = 0.0550 \text{ \AA}^{-2}$ . This treatment leads to analytic expressions for all integrals. We take the charge on each K as + electron and each C as  $-0.05$  electron.

As indicated in Fig. 1, we find that  $\lambda_Q(\omega)$  is negligible above  $200 \text{ cm}^{-1}$  and  $\lambda_Q$  has two peaks. One near  $\omega_0 \approx 20\text{--}40 \text{ cm}^{-1}$ , involves octahedral K plus  $C_{60}$  librations; whereas the other at  $\omega_T \approx 130\text{--}150 \text{ cm}^{-1}$  involves tetrahedral K.

Table 1. Definitions of quantities in Eq. 11

$\Theta = f_1 f_2 \omega_{\log}$	$\mu^* = N(0)V_c/[1 + N(0)V_c \log(E_e/\omega_{ph})]$
$f_1 = \left[ 1 + \left( \frac{\lambda}{\Lambda_1} \right)^{3/2} \right]^{1/3}$	$f_2 = 1 + \frac{\left( \sqrt{\langle \omega^2 \rangle} / \omega_{\log} - 1 \right) \lambda^2}{\lambda^2 + \Lambda_2^2}$
$\Lambda_1 = 2.46 (1 + 3.8\mu^*)$	$\Lambda_2 = 1.82 (1 + 6.3\mu^*) \left( \sqrt{\langle \omega^2 \rangle} / \omega_{\log} \right)$
$\omega_{\log} = \exp \left[ \frac{2}{\lambda} \int_0^\infty \frac{d\omega}{\omega} \alpha^2(\omega) F(\omega) \log \omega \right]$	$\langle \omega^2 \rangle = \frac{2}{\lambda} \int_0^\infty d\omega \alpha^2(\omega) F(\omega) \omega$

$E_e$  and  $\omega_{ph}$  are the characteristic energy of conduction electron and phonon, respectively, and  $V_c = \langle 4\pi e^2 / (k^2 + q_{sc}^2) \rangle$  is averaged over the Fermi surface. We take  $E_e = E_w = 0.6 \text{ eV}$  (the bandwidth) and  $\omega_{ph} = \omega_{\log}$ .

**Dynamic JT Coupling ( $H_{JT}^{ep}$ ).** Lannoo *et al.* (6, 7), Johnson *et al.* (8), and Varma *et al.* (9) suggested that JT coupling might play a role in the superconductivity, and Varma *et al.* (9) used modified neglect of differential overlap (MNDO) (20) calculations to estimate the couplings. We have repeated the estimates of Varma *et al.* (9) but using the vibrational modes from the GraFF (13) rather than from MNDO (20) (MNDO leads to frequencies  $\approx 11\%$  high). Letting  $g_m$  be the energy derivative with respect to displacement of  $m$  mode, we calculate (ref. 9 in parentheses): 0.19(0.1), 0.16(0.1), 0.26(0.2), 0.38(0.0), 0.26(0.6), 0.12(0.2), 1.77(1.8), and 1.49(1.2) for  $g_m$  of the eight  $H_g$  modes. This leads to (6–9)

$$\lambda_{JT,m} = \frac{5 N(0)}{6 M \omega_m^2} g_m^2, \quad [8]$$

shown in Fig. 1. Thus  $\lambda_{JT} = \sum_m \lambda_{JT,m} \sim \lambda_Q$  for  $R_{sc} \approx 0.6$  to  $1.0 \text{ \AA}$ .

### Calculations of $T_c$

**The Modified McMillan Equation.** McMillan (21) and then Allen and Dynes (22) succeeded in developing a general formula for how the transition temperature  $T_c$  depends on the phonon density of states and the electron–phonon coupling matrix. Starting with

$$\alpha_{\mathbf{k}}^2(\omega) F_{\mathbf{k}}(\omega) = \frac{1}{(2\pi)^3} \sum_j \int \frac{d^2 \mathbf{k}}{v_F} |M_{\mathbf{k}' \mathbf{k} j}|^2 \delta(\omega - \Omega_{\mathbf{q}j})$$

$$\alpha^2(\omega) F(\omega) = \frac{1}{(2\pi)^3} \int \frac{d^2 \mathbf{k}}{v_F} \alpha_{\mathbf{k}}^2(\omega) F_{\mathbf{k}}(\omega) / \int \frac{d^2 \mathbf{k}}{v_F} \quad [9]$$

$$\lambda = \int \lambda(\omega) d\omega = 2 \int \alpha^2(\omega) F(\omega) \frac{d\omega}{\omega}, \quad [10]$$

where  $v_F = \frac{1}{\hbar} \partial \epsilon_{\mathbf{k}} / \partial k_{\perp}$  is the average Fermi velocity ( $k_{\perp}$  is perpendicular to the Fermi surface), and  $\lambda$  is the coupling constant. They found that (21, 22)

$$T_c = \frac{\Theta}{1.20} \exp \left[ -\frac{1.04(1 + \lambda)}{\lambda - \mu^* - 0.62\lambda\mu^*} \right], \quad [11]$$

where various quantities are defined in Table 1.

### Results

Now defined are all quantities required to calculate the  $T_c$  from Eq. 11. Table 2 has the calculated superconducting

Table 2. Superconducting properties for different values of  $R_{sc}$  (the only variable in the calculations)

$R_{sc}$ (Å)	$\lambda_Q/\lambda_{JT}$	$\mu^*$	$\lambda$	$T_c$ (K)	$\Delta T_c$ (K) <sup>†</sup>	$\alpha_C$ <sup>‡</sup>	$\alpha_K$ <sup>‡</sup>
0.50	0.17	0.29	0.90	9.7	-6.4 (-3.6)	-0.10	-0.02
0.63	0.36	0.29	1.06	11.6	-8.7 (-5.8)	0.02	0.02
0.80	0.77	0.27	1.38	16.2	-9.9 (-5.3)	0.15	0.12
1.00	1.48	0.25	1.93	17.7	-5.8 (-0.5)	0.16	0.23
2.00	7.04	0.21	6.23	20.0	-0.1 (+3.2)	-0.01	0.44
Exp.				18 <sup>§</sup> , 19.3 <sup>¶</sup>	-7.2 <sup>  </sup>	0.30 (6) <sup>††</sup>	

Exp., experimental results.

<sup>†</sup>Change in  $T_c$  for pressure = 1 GPa = 10 kbar; in parentheses is the change assuming  $N(0) = 11.5$ .

<sup>‡</sup> $\alpha$  is the isotope exponent ( $T_c \propto M^{-\alpha}$ ).  $\alpha_C$  for  $^{12}C \rightarrow ^{13}C$  and  $\alpha_K$  for  $^{39}K \rightarrow ^{41}K$ .

<sup>§</sup>Ref. 1.

<sup>¶</sup>Ref. 3.

<sup>||</sup>Refs. 23–25.

<sup>††</sup>Ref. 26.

properties for various values of  $R_{sc}$ . These calculations use the density of states  $N(0) = 11.5$  from our tight-binding calculations. The susceptibility and critical field (23) suggest that  $N(0) \approx 10$ –15, whereas NMR measurement (24) gives  $N(0) \sim 20$ . An early photoemission experiment (25) reported that  $N(0) = 1.9$ , which may be low due to the surface sensitivity of these experiments.

We see that  $R_{sc} = 0.8$ –2.0 Å leads to  $T_c = 16$ –20 K, in good agreement with experiment (1–3). This does not prove the Q–JT mechanism because  $T_c$  depends sensitively upon  $N(0)$ , but neither experiment nor theory provides a precise value. The real test must be other properties.

Superconducting  $K_3C_{60}$  leads to an unusually large drop of  $T_c$  under external pressure (26),  $\Delta T_c \approx -7.2$  K for  $P = 1$  GPa. Using our force field, we calculated directly the equilibrium structure (allowing buckling of the buckyballs) and phonons for  $P = 1$  GPa and recalculated  $\lambda(\omega)$ . Here we used the LDA results (27) that  $N(0)$  decreases 20% under 1-GPa external pressure. The theory leads to  $\Delta T_c = -6$  to  $-10$  K for  $R_{sc} = 0.5$  to 1.0 Å.

A second significant test is the shift of  $T_c$  with isotope substitution. Experiments lead to  $\alpha_C = 0.30 \pm 0.06$  for  $K_3C_{60}$  (28) and  $\alpha_C = 0.37 \pm 0.05$  for  $Rb_3C_{60}$  (29) [an early report (30) of  $\alpha_C = 1.4 \pm 0.5$  may be inaccurate]. We recalculated all phonon states and  $\lambda(\omega)$  for both  $^{12}C \rightarrow ^{13}C$  and for  $^{39}K \rightarrow ^{41}K$ . The resulting  $\alpha_C = 0.15$  and 0.16 for  $R_{sc} = 0.8$  and 1.0 Å are in reasonable agreement with experiment (28–30), but  $R_{sc}$  outside this range would lead to  $\alpha_C$  in clear disagreement with experiment. A test here would be to measure  $\alpha_K$ , which we predict to be 0.12–0.23.

## Discussion

Our conclusion is that the superconductivity of  $K_3C_{60}$  is explained quite well by the Q–JT electron–phonon coupling mechanism including both  $H_{eph}^Q$  and  $H_{eph}^{JT}$  (with  $R_{sc} \approx 0.8$  to 1.0 Å). To test whether either  $H_{eph}^Q$  or  $H_{eph}^{JT}$  is sufficient, we carried out the same calculations using only one coupling.

Table 3. Effects of not having both Q coupling and JT coupling

$R_{sc}$ (Å)	Q coupling			JT coupling		
	$\delta T_c$ <sup>†</sup>	$\Delta T_c$ <sup>‡</sup>	$T_c$	$\delta T_c$ <sup>†</sup>	$\Delta T_c$ <sup>‡</sup>	$T_c$
0.50	NS	NS	NS	0.20	-0.73	1.52
0.63	0.00	NS	0.00	0.02	-0.01	0.02
0.80	0.00	-0.34	0.34	0.00	0.00	0.00
1.00	0.00	-2.26	2.50	0.00	0.00	0.00
2.00	0.00	-3.56	13.12	NS	NS	NS

All quantities are in the units of K. NS indicates not superconducting.

<sup>†</sup> $\delta T_c$  is the change for  $T_c$  upon  $^{12}C \rightarrow ^{13}C$ .

<sup>‡</sup> $\Delta T_c$  for 1 GPa pressure.

Table 3 shows that neither  $H_{eph}^Q$  nor  $H_{eph}^{JT}$  alone accounts for the superconducting properties of  $K_3C_{60}$ . With  $R_{sc} = 1.0$  Å,  $H_{eph}^Q$  leads to  $T_c = 2.5$  K, which drops for smaller  $R_{sc}$ . Larger values of  $R_{sc}$  with  $H_{eph}^Q$  alone lead to higher  $T_c$  values (e.g., 13 K for  $R_{sc} = 2.0$  Å) but  $\alpha_C \approx 0$ , in disagreement with experiment (28–30). Including only JT with  $R_{sc} = 0.5$  Å leads to  $T_c = 1.5$  K (which goes to zero for higher  $R_{sc}$ ) and a negative value of  $\alpha_C$ , also in disagreement with experiment (28–30); these results for JT alone differ from ref. 9 because they used a smaller, fixed value of  $\mu^*$ .

The conclusion here is that synergy between  $H_{eph}^Q$  and  $H_{eph}^{JT}$  leads to the special properties of buckyball superconductors. In the range  $R_{sc} = 0.8$ –1.0 Å,  $\lambda_Q/\lambda_{JT} \approx 0.8$ –1.5, so that both contributions are comparable. With only  $H_{eph}^Q$ ,  $T_c$  drops substantially because  $\lambda$  decreases and  $\omega_{log}$  becomes very small (decreasing  $\Theta$  of Eq. 11). For only JT,  $\lambda$  decreases, whereas  $\omega_{log}$  is very large, leading to a high  $\mu^*$  and, hence, a large negative exponential term in Eq. 11 and a low  $T_c$ .

The JT coupling essential to the Q–JT mechanism is large for  $C_{60}$  because of the high symmetry. Other buckyballs ( $C_{70}$ ,  $C_{76}$ ) have much lower symmetry and generally do not have a degenerate ground state (first-order JT coupling) for the anion. Because eliminating JT drops  $T_c$  from  $\sim 16$ –18 K to  $\sim 0$ –3 K, we expect other buckyballs to have  $T_c < 3$  K (potassium-intercalated graphite has  $T_c = 0.8$  K). We do not yet have a band structure for  $Rb_3C_{60}$  to fit to Eq. 3; however, we did a Q–JT calculation, assuming  $R_{sc} = 0.8$  Å, taking Fermi surface and  $\mu^*$  the same as  $K_3C_{60}$  and estimating  $N(0) = 1.2 \times 11.5$  [based on the result of an LDA calculation (27)]. Using the phonon states and optimal structure for  $Rb_3C_{60}$  from our force field (13) leads to  $T_c \approx 23.5$  K for  $Rb_3C_{60}$ , as compared with  $T_c = 16.2$  K for  $K_3C_{60}$  [experimental values (1–3) are 29 and 19 K, respectively].

Summarizing, we find that a combination of the charge and JT electron–phonon couplings are responsible for the superconductivity in  $K_3C_{60}$ . This explains  $T_c$ ,  $\Delta T_c$  (1 GPa), and  $\alpha_C$  (and predicts  $\alpha_K$ ). More definitive tests of this Q–JT mechanism will be the prediction of  $T_c$  for various mixed alkali systems (2–5) where  $T_c$  ranges from 2.5 to 33 K. There are no variables left to our disposal; thus the force fields (and hence phonons) are determined,  $R_{sc}$  must be  $\sim 0.8$ –1.0 Å, and the quantities in  $\mu^*$  are defined. The only remaining variables have to do with the electronic states [e.g.,  $N(0)$  and Fermi surface], which will emerge from LDA calculations.

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